

Answer ALL questions.

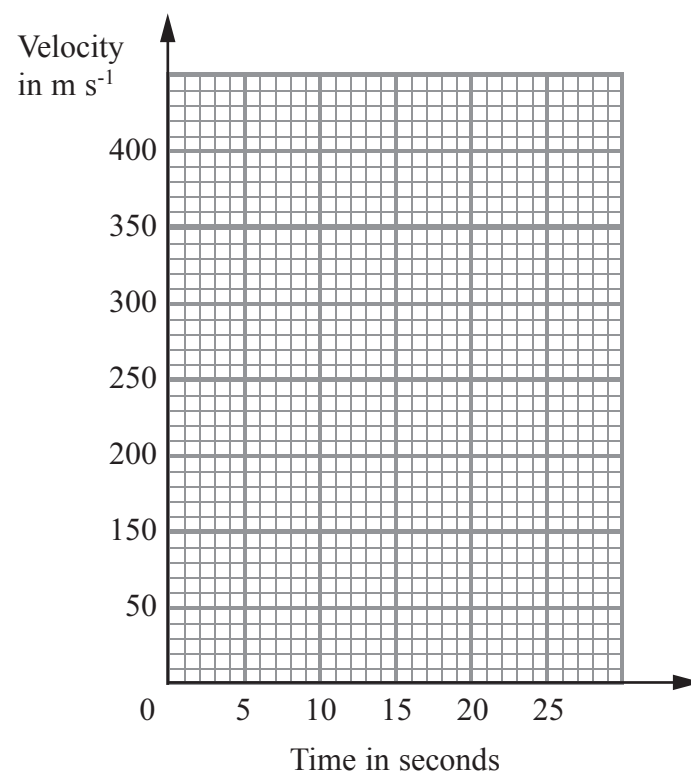
Write your answers in the spaces provided.

You must write down all stages in your working.

1. (a) The table below shows the velocity, $v \text{ m s}^{-1}$, of a projectile at time $t \text{ s}$ after it was launched from an aircraft:

Time, t (seconds)	5	10	15	20	25
Velocity, v (m s^{-1})	115	175	235	295	355

- (i) Assuming that the velocity is changing at a constant rate, plot a velocity-time graph for the projectile for the period $0 \leq t \leq 25$



(2)



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(ii) Use your graph to determine a formula for v in terms of t .

$v = \dots\dots\dots$
(2)

(b) The Work-Energy Principle can be written as:

$$W_T = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

Write down an expression for W_T in fully factorised form.

(2)



(c) The distance s m travelled by a car t seconds after passing a road sign is given by the formula

$$s = 27t + 3t^2$$

Find how long it takes the car to travel a distance of 66 m past the road sign.

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Time =s
(3)

Q1

(Total 9 marks)



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2. (a) Show, using a sketch of a right angled triangle, that if $\sin \theta = \frac{8}{17}$, where θ is an acute angle, then $\cos \theta = \frac{8}{17}$.

(3)

- (b) A voltage, v volts, in a circuit is given by the equation $v = 1 + \cos \theta$.

Sketch a graph of the voltage v over the range $\theta = 0^\circ$ to $\theta = 360^\circ$.

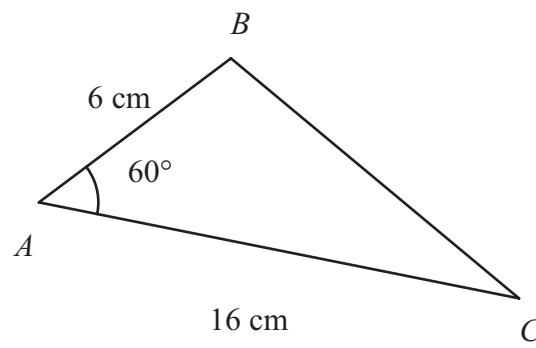
Use your graph to determine the value of voltage when $\theta = 270^\circ$.

When $\theta = 270^\circ$, $v = \dots\dots\dots$

(4)



- (c) A triangular metal plate ABC has $AB = 6$ cm, $AC = 16$ cm and angle $BAC = 60^\circ$. Find the length of BC .



$BC = \dots\dots\dots$ (3)

(Total 10 marks)

Leave blank

Q2



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3. (a) A sealed cylindrical tank has diameter 0.5 m and height 1.5 m. Find the total external surface area of the tank.

Surface area = m²
(3)

- (b) Determine the length of an arc of a circular vehicle test track given that the track has a diameter of 1.5 km and the angle subtended by the arc at the centre of the track is 120°.

Length = km
(3)



(c) A flywheel revolves at 300 rpm. Express this in radians **per second**.

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(3) Q3

(Total 9 marks)



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4. The following data was obtained (to the nearest whole number) on a batch of 199 resistors with a marked value of 100 Ω :

Actual resistance value (Ω)	96	97	98	99	100	101	102	115
Frequency	1	1	3	20	56	61	37	20

- (a) (i) Calculate, to the nearest whole number, the mean resistance value of the batch.

Mean = Ω
(4)

- (ii) Calculate the median resistance value of the batch.

Median = Ω
(3)



(b) State, with a reason, which of these two averages you would use to summarise the data.

.....
.....
.....

(2)

(Total 9 marks)

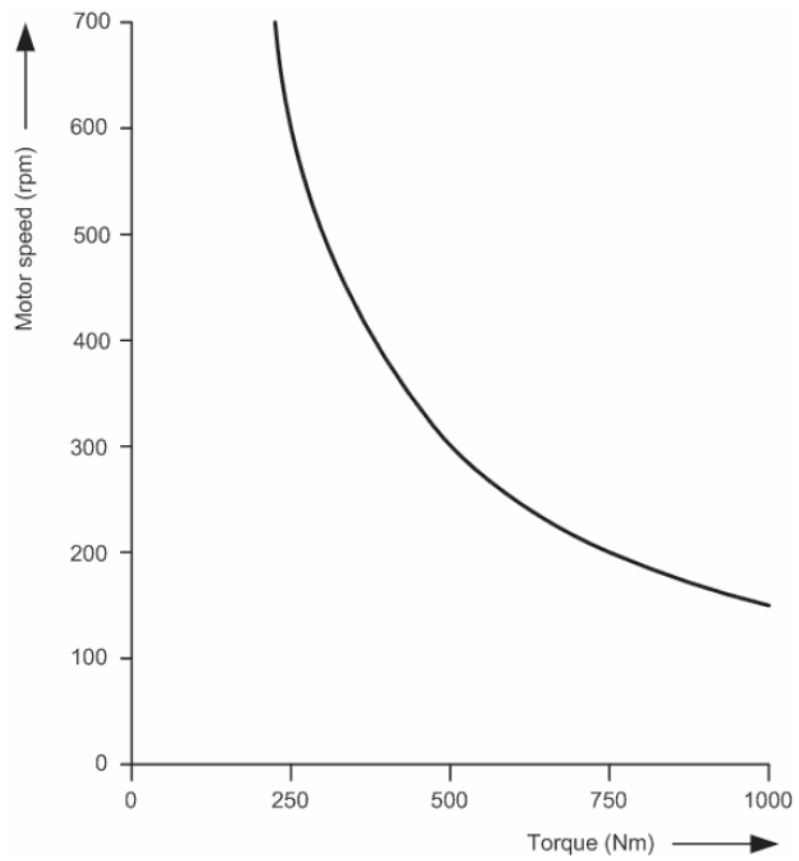
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Q4



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5.



(a) The graph above shows how the speed of a motor varies with torque.

Draw a tangent to the graph and use it to determine the rate of change of torque with speed when the torque is 500 Nm.

$\Delta T/\Delta s = \dots\dots\dots$ Nm/rpm
(3)



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(b) The velocity v of an aircraft at time t is given by the equation $v = 2t^2 + 5$

(i) Use calculus to derive an expression for the acceleration of the body at time t .

$$a = \dots\dots\dots \quad (2)$$

(ii) Find the acceleration at $t = 2$ s.

$$a = \dots\dots\dots \text{ m/s}^2 \quad (1)$$

(c) Use calculus to determine the distance travelled by the aircraft between $t = 0$ and $t = 4$ s.

$$\text{Distance} = \dots\dots\dots \text{ m} \quad (4)$$

(Total 10 marks)

Q5



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6. (a) (i) Make l the subject of the formula $t = 2\pi\sqrt{\frac{l}{g}}$

$$l = \dots\dots\dots \text{m} \quad (3)$$

(ii) Find l when $t = 2$ s and $g = 9.81$ m/s².

$$l = \dots\dots\dots \text{m} \quad (2)$$



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(b) Given that $A = 20 \log_{10} \left(\frac{V_{out}}{V_{in}} \right)$,

determine V_{out} when $V_{in} = 0.15$ and $A = 36$

$V_{out} = \dots\dots\dots$ **(4)**



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(c) The voltage developed across a capacitor is given by the relationship,

$$V_c = V \left(1 - e^{-\frac{t}{CR}} \right)$$

Determine the value of C when $V_c = 50$, $V = 100$, $R = 1 \times 10^6$, and $t = 200$

$C = \dots\dots\dots$
(4)

Q6

(Total 13 marks)

TOTAL FOR PAPER: 60 MARKS

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