

Mark Scheme (Results) November 2008

IGCSE

IGCSE Mathematics (4400) Paper 3H

November 2008 IGCSE 4400 Maths Mark Scheme - Paper 3H

Q	Working	Answer	Mark	Notes
1.	$\frac{11.7}{6.5}$		2	M1 for 11.7 or 6.5
		1.8		A1 Accept $\frac{9}{5}$ etc
				Total 2 marks

2.	(a)	$7(p - 3)$	1	B1 cao
	(b)	or $x + 5 = 3$	3	M1 for $4x + 20$ seen M1 for $4x = 12 - 20$ or for $4x = 12 - 5$ following $4x + 5 = 12$
		-2		A1
				Total 4 marks

Q	Working	Answer	Mark	Notes
3. (a)	$1 \times 10 + 2 \times 9 + 3 \times 3 + 4 \times 17 + 5 \times 11$ or $10 + 18 + 9 + 68 + 55$ or 160		3	M1 for at least 3 correct products and summing them
	$\frac{"160"}{50}$			M1 (dep) for division by 50
		3.2		A1 Accept 3 if $\frac{160}{50}$ seen
(b)(i)		$\frac{17}{50}$	3	B1 Accept 0.34 or 34%
(ii)	$\frac{10+3}{50}$ or $\frac{10}{50} + \frac{3}{50}$			M1
		$\frac{13}{50}$		A1 Accept 0.26 or 26%
(c)		'No' ticked and eg <i>The scores are not equally likely. 4 is most likely.</i>	1	B1
				Total 7 marks

4. (a)		translation	2	B1 Accept translated, translate etc	These marks are independent but award no marks if the answer is not a single transformation
	7 to the left and 1 down or $\begin{pmatrix} -7 \\ -1 \end{pmatrix}$			B1	
(b)		rotation	3	B1 Accept rotated, rotate etc	
		90°		B1 Accept quarter turn Accept 270°clockwise	
		(0, 0)		B1 Accept origin, O	
					Total 5 marks

Q	Working	Answer	Mark	Notes
5. (a)	$\frac{35}{100} \times 180$ or 63 180 – “63”	117	3	M1 M2 for $\frac{65}{100} \times 180$
				M1 dep A1 cao
			3	M2 for $\frac{84}{0.35}$ or $84 \times \frac{100}{35}$ M1 for $\frac{84}{35}$ or 2.4
(b)	$\frac{84}{0.35}$ or $84 \times \frac{100}{35}$	240	3	A1 M2 for $\frac{442}{0.65}$ or $442 \times \frac{100}{65}$ M1 for $\frac{442}{65}$ or 6.8 or 65% = 442
(c)	$\frac{442}{0.65}$ or $442 \times \frac{100}{65}$	680	3	A1 cao
				Total 9 marks

6.	$\pi \times r^2 \times 7.6$		3	M2 if $r = \frac{4.3}{2}$ or 2.15 (M1 if $r = 4.3$ may be implied by answer rounding to 441)
		110		A1 for answer rounding to 110 ($\pi \rightarrow 110.367 \dots$ 3.14 \rightarrow 110.311 ...)
				Total 3 marks

Q	Working	Answer	Mark	Notes
7.	$\frac{2}{5} \times \frac{7}{4}$ or $\frac{14}{35} \div \frac{20}{35}$		3	B2 for $\frac{2}{5} \times \frac{7}{4}$ (B1 for inverting second fraction ie $\frac{7}{4}$) or B1 for 2 fractions with a denominator of 35 etc B1 for correct numerators
				B1 eg for $\frac{14}{20}$ oe or correct cancelling
				Total 3 marks

8.			2	B1 cao
(a)(i)		p^6		
(ii)		q^5		B1 cao
(b)	$12x - 3 - 8x + 12$		2	M1 for 3 correct terms
		$4x + 9$		A1 cao
(c)	$y^2 + 5y + 3y + 15$		2	M1 for 3 correct terms or $y^2 + 8y + c$ or ... + $8y + 15$
		$y^2 + 8y + 15$		A1 cao
				Total 6 marks

Q	Working	Answer	Mark	Notes
9.	$\cos x^\circ = \frac{5.4}{8.7} \text{ or } 0.6206\dots$		3	<p>or M1 for sin and $\frac{\sqrt{46.53}}{8.7}$ following correct Pythagoras and A1 for value which rounds to 0.78</p> <p>for cos $\frac{5.4}{8.7}$ or 0.6206...</p> <p>M1 A1</p> <p>or M1 for tan and $\frac{\sqrt{46.53}}{5.4}$ following correct Pythagoras and A1 for value which rounds to 1.26</p>
		51.6		A1 for answer rounding to 51.6
				Total 3 marks

Q	Working	Answer	Mark	Notes
10. (a)		(2, 7)	2	B2 B1 for 2 B1 for 7
(b)	eg $\frac{13-1}{5-(-1)}$ or $\frac{12}{6}$ or $\frac{6}{3}$		4	M1 for clear attempt to use $\frac{\text{vertical difference}}{\text{horizontal difference}}$
	2			A1
		$y = 2x + 7$ or $y = "2" x + 7$		B2 for $y = 2x + 7$ or $y = "2" x + 7$ B1 for $y = 2x + c$ or for $y = "2" x + c$ where $c \neq 7$ or for $2x + 7$, $"2" x + 7$, $L = 2x + 7$, $L = "2" x + 7$ etc ft from their "2" only if it supported by working such as a fraction or numbers indicated on a diagram, even though it may not have gained M1 SC If no other marks scored, award B1 for $y = mx + 7$ for any m inc $m = 1$
				Total 6 marks

Q	Working	Answer	Mark	Notes
11. (a)	4	10 19 33 54	1	B1 cao
(b)		Points Curve	2	B1 Allow $\pm \frac{1}{2}$ sq ft from sensible table B1 or line segments (dep on 4 pts correct or ft correctly or 5 ordinates from (a) plotted correctly and consistently within intervals but not above end points)
(c)	27 (or $27\frac{1}{2}$) indicated on graph or stated		2	M1 for 27 (or $27\frac{1}{2}$) indicated on graph or stated
		≈ 66		A1 ft from sensible graph
				Total 5 marks

Q	Working	Answer	Mark	Notes
12. (a)	$\frac{10}{6}$ oe or $\frac{6}{10}$ oe seen		3	B1 for $\frac{10}{6}$ oe (1.666...) or $\frac{6}{10}$ oe (0.6) or $\frac{2}{3}$ (0.666...)
	$5.1 \times \frac{10}{6}$ or $5.1 \div \frac{6}{10}$ or 8.5			M1 for $5.1 \times \frac{10}{6}$ or $5.1 \div \frac{6}{10}$ or $5.1 \times \frac{2}{3}$ or 8.5
		3.4		A1 cao
(b)	(scale factor) ² eg $\left(\frac{6}{10}\right)^2$ or $\frac{36}{100}$ or $\left(\frac{10}{6}\right)^2$ or $\frac{100}{36}$		3	M1 for $\frac{1}{2} \times 6 \times 5.1 \sin \theta$ M2 for $\frac{1}{2} \times (10 + 6) \times 3.4 \sin \theta$ or $\frac{1}{2} \times 6 \times 5.1 \sin \theta$ M1 for $\frac{1}{2} \times 10 \times 8.5 \sin \theta - \frac{1}{2} \times 6 \times 5.1 \sin \theta$
	eg $100 - 36, 64, 1 - \frac{36}{100}, \frac{64}{100}$			
		$\frac{9}{16}$ oe		A1
				Total 6 marks

Q	Working	Answer	Mark	Notes
13. (a)		4.5 1.9 3.1 4.1	2	B2 for all correct (B1 for 2 or 3 correct)
(b)		Points Curve	2	B1 Allow $\pm \frac{1}{2}$ sq ft from table if at least B1 scored in (a) B1 ft from their points if at least 5 points are correct or ft correctly
(c)(i)		2	2	B1 cao
(ii)		1.6 or 1.7	B1	for answer which rounds to 1.6 or 1.7 ft from curve if B1 scored for curve in (b) Condone >1 dp
				Total 6 marks

14. (a)		$3b(3a - 4b)$	2	B2 B1 for $3(3ab - 4b^2)$ or $b(9a - 12b)$ or for two factors one of which is $3b$ or $(3a - 4b)$ and the other is linear
(b)		$8a^3b^6$	2	B1 B1 for 8 B1 for a^3b^6
				Total 4 marks

Q	Working	Answer	Mark	Notes
15. (a)	$\frac{7}{9} \times \frac{6}{8}$		2	M1
(b)	$\frac{7}{9} \times \frac{2}{8} + \frac{2}{9} \times \frac{7}{8}$	$\frac{42}{72}$ oe	3	A1 for $\frac{42}{72}$ oe inc $\frac{7}{12}$ M1 for one of correct products $\frac{7}{9} \times \frac{2}{8}$ or $\frac{2}{9} \times \frac{7}{8}$ for sum of both correct products or M2 for $1 - (a) - \frac{2}{9} \times \frac{1}{8}$ SC M1 for $\frac{7}{9} \times \frac{2}{9}$ or $\frac{2}{9} \times \frac{7}{9}$ M1 for $\frac{7}{9} \times \frac{2}{9} + \frac{2}{9} \times \frac{7}{9}$
		$\frac{28}{72}$ oe		A1 for $\frac{28}{72}$ oe inc $\frac{7}{18}$
				Total 5 marks

16. (a)(i)	54		2	B1
(ii)	angle between chord & tangent = angle in alternate segment			B1 Accept 'alternate segment'
(b)	angle $BCD = 90^\circ$		2	B1
(c)(i)	angle in a semicircle is a right angle		2	B1 Accept if 'semicircle' seen
(ii)	opposite angles of a cyclic quadrilateral are supplementary	102		B1
				Total 6 marks

Q	Working	Answer	Mark	Notes
17. (a)	$10x = 7.7$		2	M1 Accept $100x = 77.7$
(b)(i)		$\frac{7}{9}$ oe		A1
(ii)	eg $9d = 1 + \frac{y-1}{10}$ or $90d = 10 + y - 1$ or $90d = y + 9$ or $\frac{10+y-1}{90}$ or $0.1 + 0.0y$	$\frac{y}{90}$	3	B1 M1 for equation which would give a correct answer or for an expression which, if simplified would give a correct answer or for $0.1 + 0.0y$ but not for $9d = 1.y - 1$ or similar
		$\frac{9+y}{90}$ or $\frac{1}{10} + \frac{y}{90}$		A1 isw and award 2 marks if $\frac{9+y}{90}$ or $\frac{1}{10} + \frac{y}{90}$ seen
				Total 5 marks

Q	Working	Answer	Mark	Notes
18.	$\frac{2}{x+2} + \frac{x}{(x+2)(x+3)}$		5	B1 for factorising $x^2 + 5x + 6$
	$\frac{2(x+3)+x}{(x+2)(x+3)}$ or $\frac{2(x+3)}{(x+2)(x+3)} + \frac{x}{(x+2)(x+3)}$ or $\frac{2(x^2+5x+6)+x(x+2)}{(x+2)(x^2+5x+6)}$			B1 for correct single fraction even if unsimplified or for correct sum of two fractions with the same denominator ft from incorrect factorisation
	$\frac{2x+6+x}{(x+2)(x+3)} = \frac{3x+6}{(x+2)(x+3)}$ or $\frac{2x+6+x}{x^2+5x+6} = \frac{3x+6}{x^2+5x+6}$			B1 for $\frac{2x+6+x}{(x+2)(x+3)}$ or $\frac{2x+6+x}{x^2+5x+6}$
	$\frac{3(x+2)}{(x+2)(x+3)}$			B1
		$\frac{3}{x+3}$		B1 cao
				SC if no denominator, award 3 rd B1 for $2x+6+x$ and 4 th B1 for $3(x+2)$
				Total 5 marks

Q	Working	Answer	Mark	Notes
19.	$\frac{45}{360} \times \pi \times 6.7^2 - \frac{1}{2} \times 6.7^2 \times \sin 45^\circ$		5	M1 for $\frac{45}{360}$ oe
				M1 for $\pi \times 6.7^2$ or value which rounds to 141 seen
				M1 for completely correct method of finding the area of triangle OAB eg $\frac{1}{2} \times 6.7^2 \times \sin 45^\circ$ or $6.7 \times \sin 22.5^\circ \times 6.7 \times \cos 22.5^\circ$
	17.628... (or 17.619...) – 15.871...			A1 for either area correctly evaluated rounded or truncated to 1 dp
		1.76 or 1.75		A1 for answer rounding to 1.76 if π key used ($\pi \rightarrow 1.7572...$) or for answer rounding to 1.75 if $\pi = 3.14$ used ($3.14 \rightarrow 1.7483...$)
				Total 5 marks

Q	Working	Answer	Mark	Notes
20.	eg $r^2 + 9 = (r + 2)^2$ $r^2 + 3^2 = (r + 2)^2$ $r = \sqrt{(r + 2)^2 - 9}$ $r + 2 = \sqrt{r^2 + 9}$		5	M2 for correct use of Pythagoras' Rule M1 for $r^2 + 3^2$ or $r^2 + 9$ or $(r + 2)^2$
	$r^2 + 9 = r^2 + 4r + 4$			B1
	$4r = 5$			M1
		$1\frac{1}{4}$ or 1.25		A1 Accept $\frac{5}{4}$
				Total 5 marks