

Mark Scheme (Results)

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Pearson Edexcel International GCSE In Mathematics B (4MB1) Paper 01

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.

Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.

- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

• Types of mark

- M marks: method marks
- o A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

• Abbreviations

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- SC special case
- oe or equivalent (and appropriate)
- o dep dependent

- o indep independent
- o awrt answer which rounds to
- o eeoo each error or omission

• No working

If no working is shown then correct answers normally score full marks If no working is shown then incorrect (even though nearly correct) answers score no marks.

• With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review. If there is a choice of methods shown, mark the method that leads to the answer given on the answer line.

If no answer appears on the answer line, or there is no answer line, mark both methods **then award the lower number of marks**.

If there is no answer on the answer line then check the working for an obvious answer.

• Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

• Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

Question	Working	Answer	Mark	Notes
1		3.15×10^{-4}	1	B1
				Total 1 marks
2	124 + 180 oe		2	M1 $270 + 34$ commonly seen.
		304		A1
				Total 2 marks
3	$180 - 135 \text{ or } \angle BED = 45 \text{ or}$ $\angle BEF = 135 \text{ or } \angle DEH = 135 \text{ or}$ $\angle CBE = 45 \text{ or } \angle CBE = p \text{ or}$ $135 + p = 180 \text{ or } \frac{360 - 2 \times 135}{2}$		2	M1 Allow values marked on the diagram
		45(°)		Al
				Total 2 marks
4	$\frac{15}{8} \times \frac{13}{5} \text{ or } \frac{1 \times 8 + 7}{8} \times \frac{2 \times 5 + 3}{5}$		2	M1 Or equivalent method for multiplying two fractions
		$4\frac{7}{8}$		A1 Dependent on M mark being awarded.
				Total 2 marks
5 (a)		10, 14, 16, 18, 20, 22, 26, 28	2	B1 Ignore brackets
(b)		2		B1 Ignore brackets
				Total 2 marks

Question	Working	Answer	Mark	Notes
6	Rearranging scores in ascending/ descending order (at least seven in order) 3,6,11,18,23,23,26,45,56,56,78,87 or 23 and 26 identified		2	M1
		24.5		A1 Accept $\frac{49}{2}$
7			2	Total 2 marksM1 for 2 correct terms or k , $k - 5$, $k - 10$ (where k is an integer)
		-13,-18,-23		A1 Total 2 marks
8	$\frac{42}{5\times 60}$ (= 0.14) oe		3	M1 $\frac{42}{300}$ or $\frac{0.7}{5}$
	$\left\ \frac{42}{5\times60}\right\ \times 100$			M1 indep Allow for $\frac{42}{a} \times 100$ or $\frac{b}{5} \times 100$ for any a or b $\neq 1$
		14		A1
				Total 3 marks
9 (a)	Correct circle around one of $x = -3$ or $x = 4$ and corresponding line drawn in the correct direction or Line joining $x = -3$ and $x = 4$		2	M1
		Both end points identified using the correct symbols and one correct line drawn between the two correct points.		A1 -3 -2 -1 0 1 2 3 4
(b)		-3, -2, -1, 0, 1, 2, 3		B1
				Total 3 marks

Que	stion	Working	Answer	Mark	Notes
10	(a)		$\begin{pmatrix} 7 & -3 \\ 8 & -1 \end{pmatrix}$	3	B1
			$\begin{pmatrix} -16 & -6 \\ -8 & 10 \end{pmatrix}$		B2 Fully correct B1 for 2 or 3 correct elements in a 2×2 matrix
					Total 3 marks
11		$\frac{5(2+5x)-2(3-2x)}{(3-2x)(2+5x)}$ (oe)		3	M1 for correct single fraction
		$\frac{10 + 25x - 6 + 4x}{(3 - 2x)(2 + 5x)}$			Indep M1 for expansion of the correct numerator in single fraction Must be part of a fraction but ignore denominator for this mark. Allow a maximum of one arithmetic or sign error
			$\frac{4+29x}{(3-2x)(2+5x)}$ oe		A1 allow $6+11x-10x^2$ in the denominator do not ISW for this mark.
					Total 3 marks

Question	Working	Answer	Mark	Notes
12	$4x^3 - 8x^2 - 12x = (2x + k)Q(x)$		3	B1 Eliminate 11 from both sides allow Qx rather than $Q(x)$
	Method 1 4x(x-3)(x+1) or $x(2x-6)(2x+2)or (2x+2)(2x^2-6x) orx(4x-12)(x+1)$ or $x(x-3)(4x+4)$			M1 Factorise to three linear terms or take out $(2x + 2)$ as common factor. To award this mark their factors must expand to give 2 out of the 3 terms correct
	Method 2 2a + 2k = -8 and $ak = -12$ or 2a + 2k = -8 and $ak + 2b = -12$ and kb = 0 oe			(M1) Equate coefficients after expanding $(2x + k)Q(x)$
	Method 3 $4\left(\frac{-k}{2}\right)^3 - 8\left(\frac{-k}{2}\right)^2 - 12\left(\frac{-k}{2}\right) = 0 \text{ oe}$			(M1) use factor theorem with $x = -\frac{k}{2}$
	Method 4 $k^2 + 4k - 12 = 0$ oe			(M1) use long division equate remainder to zero
		<i>k</i> = 2		A1 NB $k = 2$ seen with no incorrect statements scores all 3 marks. $k = -6$ and k = 0 lose this final mark only.
				Total 3 marks
13	$\frac{27x^6y^9}{9xy^2}$		3	M1 Expansion of numerator – at least two components correct
		"3" "x ⁵ " "y ⁷ "		M1 indep. Correct division from their numerator with at least two components correctly following through.
		$3x^5y^7$		A1 Fully correct
				Total 3 marks

Quest	tion	Working	Answer	Mark	Notes
14		12x + 8y = 32 or $27x + 18y = 72$		4	M1 Fully correct method to obtain equation in a
		$-12x + 27y = 66 \qquad -8x + 18y = 44$			single variable.
		-12x + 27y = 66 -8x + 18y = 44 35y = 98 35x = 28 or			Allow a maximum of 1 arithmetic or sign error.
		$x = \frac{8-2y}{3}$ giving $-4\left(\frac{8-2y}{3}\right) + 9y = 22$ or			
		$x = \frac{9y-22}{4}$ giving $3\left(\frac{9y-22}{4}\right) + 2y = 8$ or			
		$y = \frac{8-3x}{2}$ giving $-4x + 9\left(\frac{8-3x}{2}\right) = 22$ or			
		$y = \frac{4x+22}{9}$ giving $3x + 2\left(\frac{4x+24}{9}\right) = 8$			
			$x = \frac{4}{5}$ or $y = \frac{14}{5}$		A1 Allow $x = 0.8$ or $y = 2.8$
		eg			M1 dep Fully correct method to obtain equation in
		$3 \times \frac{4}{5} + 2y = 8$ or $3x + 2 \times \frac{14}{5} = 8$			the other variable following through their first result.
			$x = \frac{4}{5}$ and $y = \frac{14}{5}$		A1 Allow $x = 0.8$ and $y = 2.8$
					Total 4 marks
15			$y \ge 6 - 2x$	4	B1 Allow strict inequalities
			$y \le 5 + x$		B1 Allow strict inequalities
		Method to find point of intersection of $y = 6 - 2x$ with the x-axis. Eg $6 - 2x = 0$			M1 Allow $(3,0)$ or $x = 3$ stated
		seen			
			<i>x</i> ≤ 3		A1
					SC Allow a total of B2 for
					$y \le 6 - 2x, y \ge 5 + x \text{ and } x \ge 3$
					Total 4 marks

Question	Working	Answer	Mark	Notes
16	$400^2: 3^2 \text{ or } \left(\frac{400}{3}\right)^2 \text{ or } \left(\frac{3}{400}\right)^2$		4	M1 state or use scale factor squared
	$7200 \times \left(\frac{400}{3}\right)^2$ or $\left(\frac{3}{400}\right)^2 = \frac{7200}{x}$ oe			M1 dep correct method to find surface area M2 for of ship condone $72 \times \left(\frac{400}{3}\right)^2$ $0.72 \times \left(\frac{400}{3}\right)^2$
	$\div 100^{2}$			M1 indep convert from cm^2 to m^2
		12800		A1
				Total 4 marks
17	$(BD^{2}=)6.5^{2}-2.5^{2} (=36)$ Area of $ABD = \frac{1}{2}(2.5)(BD)(=7.5)$ Area of $BCD = \frac{1}{2}(4.2)(BD) \sin 35$ (=7.23) Area of $ABCD = \frac{1}{2}(2.5)(BD) + \frac{1}{2}(4.2)(BD) \sin 35$		4	M3 Completely correct method to find area <i>ABCD</i> or M2 Completely correct method to find the area of <i>ABD</i> or <i>BCD</i> or M1 Correct method to find <i>BD</i> or <i>BD</i> ² For Area of <i>ABD</i> allow $\frac{1}{2}(6.5)(2.5) \sin BAD$ with $\cos BAD = \frac{2.5}{6.5}(BAD = 67.4)$
		awrt 14.7		A1
				Total 4 marks
18	$ \mathbf{p} ^2 = x^2 + (2x-1)^2$ and $ \mathbf{q} ^2 = (-9)^2 + 5^2$		4	M1 Attempt at both moduli or both moduli squared (or equivalent)
	$ \mathbf{p} = \mathbf{q} \Longrightarrow 5x^2 - 4x - 105 \ (=0)$			M1 dep. Forming three term quadratic in x allow a maximum of 1 arithmetic or sign error
	(5x+21)(x-5)(=0)			M1 dep. Factorising trinomial quadratic expression must expand to give 2 of 3 terms correct or completely correct substitution into a completely correct formula.
		$x = -\frac{21}{5}$ (oe)		A1 Do not allow if $x = 5$ given and not rejected allow -4.2
				Total 4 marks

Ques	tion	Working	Answer	Mark	Notes
19		$\frac{30}{360}(2\pi)(OB)$ or $\frac{30}{360}(2\pi)(OA)$ (oe)		4	M1 Allow $OA = r$ or $\frac{1}{2}r$ or $OB = r$ or $2r$
		360 360			Allow any variable used in place of r
		$\frac{30}{360} (2\pi) (2(OA)) + \frac{30}{360} (2\pi) (OA) + 2(OA) = 10$			M1 dep. Deriving an equation in a single
		$360^{(2\pi)(2(0\Pi))+}360^{(2\pi)(0\Pi)+2(0\Pi)+10}$			unknown must include all 4 sides of the
		(oe)			shape.
		$\frac{1}{2}\pi OA + 2OA = 10(\text{oe})$			M1 Simplify to equation of the form
		2			$a\pi OA + bOA = c$ or $a\pi OB + bOB = c$
					Where $a, b, c \neq 0$
			20		A1 ISW final answer given as a decimal
			$\frac{20}{4+\pi}$ oe		
					Total 4 marks
20	(a)		$14 < T \le 17$	5	B1 Condone any indication of interval 14
	. /				to 17 (eg 14< <i>T</i> <17 or 14 to 17)
	(b)	Use of at least 3 correct midpoints			M1
		$\sum fT = 6.5 \times 3 + 9.5 \times 12 + 12.5 \times 12 + 15.5 \times 16 + $			M1 indep values of <i>T</i> in the interval,
		$\overline{18.5 \times 6} + 21.5 \times 1 (=664)$			including ends and used consistently (eg
		or $\Sigma fT = 19.5 + 114 + 150 + 248 + 111 + 21.5$			all lowest value) allow one
					error/omission
		"6.5×3+9.5×12+12.5×12+			M1 dep Depends on previous M mark.
		$\frac{15.5 \times 16 + 18.5 \times 6 + 21.5 \times 1''}{50}$ (=13.28)			
		50	13		A1 cao
					Total 5 marks

Que	stion	Working	Answer	Mark	Notes
21	(a)		$g(x) \ge 1$	5	B1 Allow <i>y</i> or <i>g</i> but not <i>x</i> . Allow set notation but must indicate ≥ 1
	(b)	gf(2) = g(1) or $2(3 \times 2 - 5)^2 + 1$ or 2(3x - 5) ² + 1			M1 Correct order. An answer of 3 with no incorrect working implies this mark
		gf(2) = 3			A1
		3x - 5 = 3			M1 Dep.
			$x = \frac{8}{3}$ oe		A1 Allow 2.67 or better ISW further rounding
					Total 5 marks
22		UB: <i>a</i> = 8.455, <i>b</i> = 1.935, <i>c</i> = 3.4155		5	M1 Any two correct UB seen
		LB: <i>a</i> = 8.445, <i>b</i> = 1.925, <i>c</i> = 3.4145			M1 Any two correct LB seen
		$UB = \sqrt{\frac{"8.455" - "1.925"}{"3.4145"}}$			M1 indep Must use 8.45< <i>a</i> ≤8.455, 1.925≤ <i>b</i> <1.93 and 3.4145≤ <i>c</i> <3.415
		$LB = \sqrt{\frac{"8.445" - "1.935"}{"3.4155"}}$			M1 indep Must use 8.445≤ <i>a</i> <8.45, 1.93< <i>b</i> ≤1.935 and 3.415< <i>c</i> ≤3.4155
		UB = 1.382907, LB = 1.380585	1.38		A1 Must see both values given to at least 3 d.p
					Total 5 marks

Que	stion	Working	Answer	Mark	Notes
23	(a)	a(10-25b) or $5(2a-5ab)$		6	M1
			5a(2-5b)		A1
					Do not ISW
	(b)		(x-5)(x+2)		M1 Factorised expression that expands to
					give 2 of 3 terms correct
					A1 cao
					Do not ISW
	(c)	$2(25x^2-36y^2)$ or $(10x-12y)(5x+6y)$ or			M1
		(10x + 12y)(5x - 6y)			
			2(5x-6y)(5x+6y)		A1
			2(3x + 0y)(3x + 0y)		Do not ISW
					Total 6 marks
24		$x = 2kx^2 + 10x - 3kx - 15$		6	M1 Expanding numerator achieving a
		$y = \frac{1}{x}$			minimum of 3 correct terms in numerator
		$y = \frac{2kx^2 + 10x - 3kx - 15}{x}$ $y = 2kx + 10 - 3k - \frac{15}{x}$			M1 dep Dividing through by <i>x</i>
		x x			Also allow for a correct application of
					product or quotient rule
		$\frac{dy}{dr} = 2k + \frac{15}{r^2}$			M1 dep Differentiate. At least one non-
		$dx = 2k + x^2$			constant term correctly differentiated.
					A1 cao must follow from fully correct
					working
		$2k + \frac{15}{\left(\frac{1}{2}\right)^2} = 0$			M1 indep Set their $\frac{dy}{dx}$ equal to zero and
		(2)			substitute $x = \frac{1}{2}$
			k = -30		A1 cao must follow from fully correct
					working
					Total 6 marks

Que	stion	Working	Answer	Mark	Notes
25	(a)	(∠ADC=)180-116(=64)		7	M1
		(∠ <i>OAD</i> =)"64"–40			M1 dep ft their $ADC < 90$
			24		A1 NB Do not ISW if 24 followed by
					further values.
			Opposite angles in a cyclic		A1 Emboldened text represents the
			quadrilateral sum to 180		minimum required dependent on both
			and base angles of an		method marks.
			isosceles triangle are equal		
	(b)	$\angle AOD = 180 - 2('24')(=132)$			M1
			66		A1 ft follow through their answer to
					$\angle OAD < 90$
			Angles in a triangle sum to		A1 Emboldened text represents the
			180 and angle at the centre		minimum required.
			is twice the angle at the		Allow double instead of twice
			circumference		Allow half angle at circumference is
					angle at centre
					Total 6 marks

Question	Working	Answer	Mark	Notes
26	$ \begin{array}{c} 15 - x, x, 9 - x, 12 \text{ seen on Venn diagram} \\ \hline (T) \\ (15 - x) \\ x 9 - x \\ 12 \end{array} $ or $ 15 - x + x + 9 - x + 12 = 30 \text{ oe} \end{array} $		6	M1 Venn diagram or setting up an equation in one variable. May be inferred from $x = 6$ seen.
	(x=) 6			A1 Value may be seen in Venn diagram
	$\frac{"6"}{9}$ seen			M1 dep May be embedded in working
	$\frac{\frac{6}{9}}{9} \times \frac{6}{8} \times \frac{9}{7} \times \frac{9}{7} = \frac{5}{18} \text{ oe}$			M1 dep May be embedded in working allow numerators and denominators in any order
	$3 \times \frac{{}^{"6"}}{9} \times \frac{{}^{"6"-1}}{8} \times \frac{9 - {}^{"6"}}{7}$ oe			M1 dep Fully correct expression. Allow numerators and denominators in any order
		$\frac{15}{28}$		A1 awrt 0.536
				Total 6 marks

Questio	n Working	Answer	Mark	Notes
27	$AB = AO + OB = -3\mathbf{a} + 5\mathbf{b}$		5	B1 may be embedded within working
	$\overset{\text{unr}}{AC} = \frac{3}{4} ("-3\mathbf{a} + 5\mathbf{b}") \text{ oe } \mathbf{or} \overrightarrow{BC} = -\frac{1}{4} ("-3\mathbf{a} + 5\mathbf{b}") \text{ oe}$			M1
	$\begin{array}{c} \begin{array}{c} \begin{array}{c} unr & unr & unr \\ OC = OA + AC = 3\mathbf{a} + \frac{3}{4} ("-3\mathbf{a} + 5\mathbf{b}") & \text{oe or} \\ \\ \begin{array}{c} unr & unr & unr \\ OC = OB + BC = 5\mathbf{b} & -\frac{1}{4} ("-3\mathbf{a} + 5\mathbf{b}") & \text{oe or} \\ \\ \begin{array}{c} unr & unr & unr \\ OD = OB + BD = 5\mathbf{b} + \frac{7}{4}\mathbf{a} + \frac{15}{4}\mathbf{b} & \text{oe or} \\ \\ \begin{array}{c} unr & unr & unr \\ CD = CB + BD = \frac{1}{4} ("-3\mathbf{a} + 5\mathbf{b}") + \frac{7}{4}\mathbf{a} + \frac{15}{4}\mathbf{b} & \text{oe} \end{array} \end{array}$			M1 $(\overrightarrow{OC} = \frac{3}{4}\mathbf{a} + \frac{15}{4}\mathbf{b})$ $(\overrightarrow{OD} = \frac{7}{4}\mathbf{a} + \frac{35}{4}\mathbf{b})$ $(\overrightarrow{CD} = \mathbf{a} + 5\mathbf{b})$ Finding any one of \overrightarrow{OC} , \overrightarrow{OD} or \overrightarrow{CD} Only follow through their result for \overrightarrow{AB}
				M1 Finding a second vector from \overrightarrow{OC} , \overrightarrow{OD} or \overrightarrow{CD} Only follow through their result for \overrightarrow{AB}
		3:4 oe		A1 Allow any equivalent numerical ratio eg. $\frac{3}{4}$: 1 PTO for alternative methods

Question	Working	Answer	Mark	Notes
27 ALT 1	$\overrightarrow{OC} = 3\mathbf{a} + \mu(-3\mathbf{a} + 5\mathbf{b})$			(B1) $-3\mathbf{a}+5\mathbf{b}$ seen
				(M1) Correct expression for \overrightarrow{OC}
	$\overrightarrow{OC} = \lambda(\mathbf{a} + 5\mathbf{b})$			(M1)
	$\lambda = \frac{3}{4}$			(M1)
		3:4 oe		(A1) Allow any equivalent numerical ratio eg. $\frac{3}{4}$: 1
27 ALT 2	$\overrightarrow{OC} = 3\mathbf{a} + \mu(-3\mathbf{a} + 5\mathbf{b})$			(B1) $-3\mathbf{a}+5\mathbf{b}$ seen
				(M1) Correct expression for \overrightarrow{OC}
	$\overrightarrow{OC} = \lambda \left(\frac{7}{4} \mathbf{a} + \frac{35}{4} \mathbf{b} \right)$			(M1)
	$\lambda = \frac{3}{7}$			(M1)
		3:4 oe		(A1) Allow any equivalent numerical ratio eg. $\frac{3}{4}$: 1
				Total 5 marks

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