M4.1 Probability and Venn diagrams				
Before you start	Why do this?			
 You should be able to: draw and interpret Venn diagrams find the probability that an event will occur. 	Venn diagrams can be used to help work out probabilities.			
Objective	🕜 Get Ready			
 You will be able to use set notation to describe events. You will be able to use Venn diagrams to find probabilities. 	 A bag contains 3 red, 2 blue and 6 green counters. A counter is taken at random. What is the probability that the counter is: 1 red 2 green 3 not green 4 blue or green 5 white 			

🔨 Key Points

When working out probabilities from a Venn diagram:

- \blacksquare P(A) represents the probability that the item is in set A
- P(A') represents the probability that the item is *not* in set A
- P(A') = 1 P(A)
- $P(A \cap B)$ represents the probability that the item is in both set A and set B
- $P(A \cup B)$ represents the probability that the item is in set A or in set B or in both sets.



Chapter 4 Probability and Venn diagrams



Methods 4.1 Probability and Venn diagrams



Exercise 4B

Some students were asked if they played tennis or cricket.



The Venn diagram shows information about their answers. A student is chosen at random. Work out:

a P(T) b P(C) c $P(T \cap C)$

A01

C AO1	2	In a group of 42 people, 13 belong to a badminton club, 19 belong to a tennis club and 7 belong to both a badminton and a tennis club.
		a Draw a Venn diagram to represent this information.
		A person is chosen at random from this group.
		b Find the probability that this person:
		I does not belong to a badminton club
		iii belongs to a tennis club but not a badminton club
B A03	3	There are 26 students in a tutor group. Of these students 11 study History, 17 study PE and 6 students study both History and PE. A student is chosen at random. Work out the probability that this student studies:
		a History b PE c History but not PE d neither History nor PE.
A03	4	There are 37 cars parked in a car park. 12 of the cars are red, 22 of the cars are Fords and 8 of the cars are red Fords. One of the cars in the car park is chosen at random. What is the probability that it is: a not red b a red car that is not a Ford c neither red nor a Ford?
A A03	5	There are 29 students in a music class. 13 can play the guitar, 8 can play the piano,
		10 cannot play the guitar and cannot play the piano.
		One of the 29 students is chosen at random.
		Work out the probability that this student can play the guitar but not the piano.
B	6	There are 120 people watching a film.
A03		68 have popcorn,
		29 have popcorn and a drink,
		35 have neither popcorn nor a drink.
		One of these people is chosen at random. Work out the probability that this person has a drink but
		does not have any popcorn.
A03	7	In a group of 35 girls 6 wear glasses, 17 have brown hair and 2 girls have brown hair and wear glasses. One of these girls is chosen at random. Work out the probability that she:
		a has brown hair but does not wear glasses
		b does not have brown hair and does not wear glasses.

M4.2 Compound events				
O Before you start	Why do this?			
You should be able to: • add and multiply fractions.	Set notation can be used to describe the probability of two events occurring at the same time.			
Objectives	O Get Ready			
 You will be able to use set notation to describe compound events. 	 A fair dice is thrown. Work out the probability of throwing: a 1 or a 2 b either an even number or a prime number. Two fair dice are thrown together. The scores are added together. Work out the probability of throwing: a total of 3 b a total of 7. 			

Kev Points	

• Two events are mutually exclusive when they cannot occur at the same time. For mutually exclusive events *A* and *B*:

 $\mathsf{P}(A \cup B) = \mathsf{P}(A) + \mathsf{P}(B)$

 $\circledast\,$ Two events are independent if one event does not affect the other event.

For two independent events A and B:

 $\mathsf{P}(A \cap B) = \mathsf{P}(A) \times \mathsf{P}(B)$

Wor	rk out P($M \cup N$).	
$M(M \cup N) = \frac{4}{9} + \frac{1}{3}$ = $\frac{4}{9} + \frac{3}{9}$	$\leftarrow \qquad \qquad M \text{ and } N \text{ are mutually exclusive events.} \\ \text{So use } P(M \cup N) = P(M) + P(N) \\ \end{aligned}$	
7		
$=\frac{1}{9}$		
= j xample 4 A di Ever	ice and a coin are thrown. nt F is getting a 5 on the dice. Event H is getting a head on the coin.	
= 🤤 xample 4 A di Ever Wor	ice and a coin are thrown. nt <i>F</i> is getting a 5 on the dice. Event <i>H</i> is getting a head on the coin. rk out:	
= ġ xample 4 A di Ever Wor a P	ice and a coin are thrown. nt F is getting a 5 on the dice. Event H is getting a head on the coin. rk out: P(F) b P(H) c P(F \cap H).	
$= \frac{1}{9}$ xample 4 A di Even Wor a P $P(F) = \frac{1}{6}$	ice and a coin are thrown. nt F is getting a 5 on the dice. Event H is getting a head on the coin. rk out: $P(F)$ b $P(H)$ c $P(F \cap H)$.	

Chapter 4 Probability and Venn diagrams

Exercise 4C C AO1 A bag contains 5 red, 3 green and 4 yellow counters. Event R is getting a red counter. Event G is getting a green counter. Event Y is getting a yellow counter. A counter is taken at random from the bag. Work out: a P(R)**b** P(G)c P(Y)d $P(R \cup Y)$ e $P(G \cup Y)$ 2 A bag contains 3 red and 4 blue counters. A01 A box contains 2 red and 5 blue counters. Event A is getting a red counter from the bag. Event B is getting a red counter from the box. One counter is taken at random from the bag and another counter is taken at random from the box. Work out: a P(A)**b** P(*B*) c $P(A \cap B)$ B A03 The events A and B are mutually exclusive. Given that $P(A) = \frac{1}{3}$ and $P(B) = \frac{5}{8}$ work out: a P(A')**b** $P(A \cup B)$ The events A and B are independent. A03 Given that $P(A) = \frac{2}{5}$ and $P(B) = \frac{1}{4}$ work out: a P(B') **b** $P(A \cup B)$ The events D and E are mutually exclusive. A03 Given that $P(D) = \frac{2}{5}$ and $P(D \cup E) = \frac{3}{4}$ work out: a P(D')**b** P(E) $P(C) = \frac{1}{4}, P(D) = \frac{2}{5}, P(C \cap D) = \frac{1}{10}$ A A03 6 Are events C and D independent? You must give a reason for your answer. 7 $P(E) = \frac{1}{4}$, $P(F) = \frac{2}{5}$, $P(E \cup F) = \frac{7}{10}$ A03 Are events E and F mutually exclusive? You must give a reason for your answer. 8 The event X and Y are independent. A03 Given that $P(X) = \frac{3}{8}$ and $P(X \cap Y) = \frac{9}{44}$ work out P(Y').



- P(A) represents the probability that the item is in set A.
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- P(A') = 1 P(A)
- $P(A \cap B)$ represents the probability that the item is in both set A and set B.
- $P(A \cup B)$ represents the probability that the item is in set A or in set B or in both sets.
- Two events are mutually exclusive when they cannot occur at the same time.

For mutually exclusive events A and B:

 $\mathsf{P}(A \cup B) = \mathsf{P}(A) + \mathsf{P}(B)$

• Two events are independent if one event does not affect the other event.

For two independent events A and B: $P(A \cap B) = P(A) \times P(B)$

Chapter 4 Probability and Venn diagrams

Answers

Chapter 4

M4.1 Get Ready answers

- **1** $\frac{3}{11}$ **2** $\frac{6}{11}$
- **3** $\frac{5}{11}$
- **4** $\frac{8}{11}$
- " 11 F 0
- **5** 0

Exercise 4A



Exercise 4B



M4.2 Get Ready answers

1	а	$\frac{1}{3}$	b	$\frac{5}{6}$
2	а	$\frac{1}{18}$	b	$\frac{1}{6}$

Exercise 4C

1	а	<u>5</u> 12	b	$\frac{1}{4}$		C	$\frac{1}{3}$
	d	$\frac{3}{4}$	е	$\frac{7}{12}$			
2	а	$\frac{3}{7}$	b	$\frac{2}{7}$		C	$\frac{6}{49}$
3	а	$\frac{2}{3}$	b	$\frac{23}{24}$			
4	а	$\frac{3}{4}$	b	$\frac{11}{20}$			
5	а	$\frac{3}{5}$	b	$\frac{7}{20}$			
6	Yes as $\frac{1}{4} \times \frac{2}{5} = \frac{1}{10}$						
7	N	$as \frac{1}{4}$ -	$+\frac{2}{5}=$	13 20			
8	P($Y') = \frac{1}{1}$	5 1				