Surname	Other n	ames
Pearson Edexcel GCE	Centre Number	Candidate Number
Mechanics M4		
Advanced/Advan	ced Subsidiary	
Wednesday 15 June 201 Time: 1 hour 30 minut	•	Paper Reference <b>6680/01</b>

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Whenever a numerical value of g is required, take  $g = 9.8 \text{ m s}^{-2}$ , and give your answer to either two significant figures or three significant figures.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information

- The total mark for this paper is 75.
- The marks for each question are shown in brackets
   use this as a quide as to how much time to spend on each question.

## **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

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1.

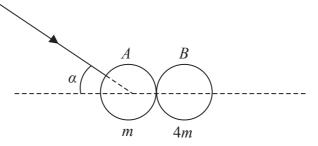


Figure 1

A smooth uniform sphere A of mass m is moving on a smooth horizontal plane when it collides with a second smooth uniform sphere B, which is at rest on the plane. The sphere B has mass A and the same radius as A. Immediately before the collision the direction of motion of A makes an angle  $\alpha$  with the line of centres of the spheres, as shown in Figure 1. The direction of motion of A is turned through an angle of  $90^{\circ}$  by the collision and the coefficient of restitution between the spheres is  $\frac{1}{2}$ 

Find the value of $\tan \alpha$ .	3)

Question 1 continued	Leave blank
	Q1
(Total 8 marks)	



2.

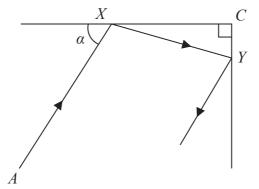


Figure 2

A small spherical ball P is at rest at the point A on a smooth horizontal floor. The ball is struck and travels along the floor until it hits a fixed smooth vertical wall at the point X. The angle between AX and this wall is  $\alpha$ , where  $\alpha$  is acute. A second fixed smooth vertical wall is perpendicular to the first wall and meets it in a vertical line through the point C on the floor. The ball rebounds from the first wall and hits the second wall at the point Y. After P rebounds from the second wall, P is travelling in a direction parallel to XA, as shown in Figure 2. The coefficient of restitution between the ball and the first wall is e. The coefficient of restitution between the ball and the second wall is e.

Find the value of $k$ .	

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Question 2 continued		

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	Q2
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3.	Two straight horizontal roads cross at right angles at the point $X$ . A girl is running, with constant speed 5 m s <sup>-1</sup> , due north towards $X$ on one road. A car is travelling, with constant speed 20 m s <sup>-1</sup> , due west towards $X$ on the other road.
	(a) Find the magnitude and direction of the velocity of the car relative to the girl, giving the direction as a bearing.
	(6)
	At noon the girl is 150 m south of $X$ and the car is 800 m east of $X$ .
	(b) Find the shortest distance between the car and the girl during the subsequent motion. (7)



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- 4. A particle P of mass 9 kg moves along the horizontal positive x-axis under the action of a force directed towards the origin. At time t seconds, the displacement of P from O is x metres, P is moving with speed v m s<sup>-1</sup> and the force has magnitude 16x newtons. The particle P is also subject to a resistive force of magnitude 24v newtons.
  - (a) Show that the equation of motion of P is

$$9\frac{d^2x}{dt^2} + 24\frac{dx}{dt} + 16x = 0$$
(4)

It is given that the general solution of this differential equation is

$$x = e^{-\frac{4}{3}t} \left( At + B \right)$$

where *A* and *B* are arbitrary constants.

When  $t = \frac{3}{4}$ , P is travelling towards O with its maximum speed of  $8e^{-1}$  m s<sup>-1</sup> and x = d.

(b) Find the value of d.

**(3)** 

(c) Find the value of x when t = 0

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Question 4 continued	

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	Q4
(Total 12 marks)	



**(5)** 

5. A toy car of mass 0.5 kg is attached to one end A of a light elastic string AB, of natural length 1.5 m and modulus of elasticity 27 N. Initially the car is at rest on a smooth horizontal floor and the string lies in a straight line with AB = 1.5 m. The end B is moved in a straight horizontal line directly away from the car, with constant speed u m s<sup>-1</sup>. At time t seconds after B starts to move, the extension of the string is t metres and the car has moved a distance t metres. The effect of air resistance on the car can be ignored.

By modelling the car as a particle, show that, while the string remains taut,

(a) (i) 
$$x + y = ut$$
 (2)

(ii) 
$$\frac{d^2x}{dt^2} + 36x = 0$$
 (4)

- (b) Hence show that the string becomes slack when  $t = \frac{\pi}{6}$  (3)
- (c) Find, in terms of u, the speed of the car when  $t = \frac{\pi}{12}$  (3)
- (d) Find, in terms of u, the distance the car has travelled when it first reaches end B of the string.



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**6.** 

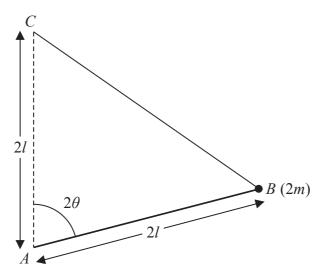


Figure 3

Figure 3 shows a uniform rod AB, of length 2l and mass 4m. A particle of mass 2m is attached to the rod at B. The rod can turn freely in a vertical plane about a fixed smooth horizontal axis through A. One end of a light elastic spring, of natural length 2l and modulus of elasticity kmg, where k > 4, is attached to the rod at B. The other end of the spring is attached to a fixed point C which is vertically above A, where AC = 2l. The angle BAC is  $2\theta$ , where  $\frac{\pi}{6} < \theta \le \frac{\pi}{2}$ 

(a) Show that the potential energy of the system is

$$4mgl\{(k-4)\sin^2\theta - k\sin\theta\} + \text{constant}$$
(6)

Given that there is a position of equilibrium with  $\theta \neq \frac{\pi}{2}$ 

(b) show that k > 8

**(6)** 

Given that k = 10

(c) determine the stability of this position of equilibrium.

(4)



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	TOTAL FOR PAPER: 75 MARKS	
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