

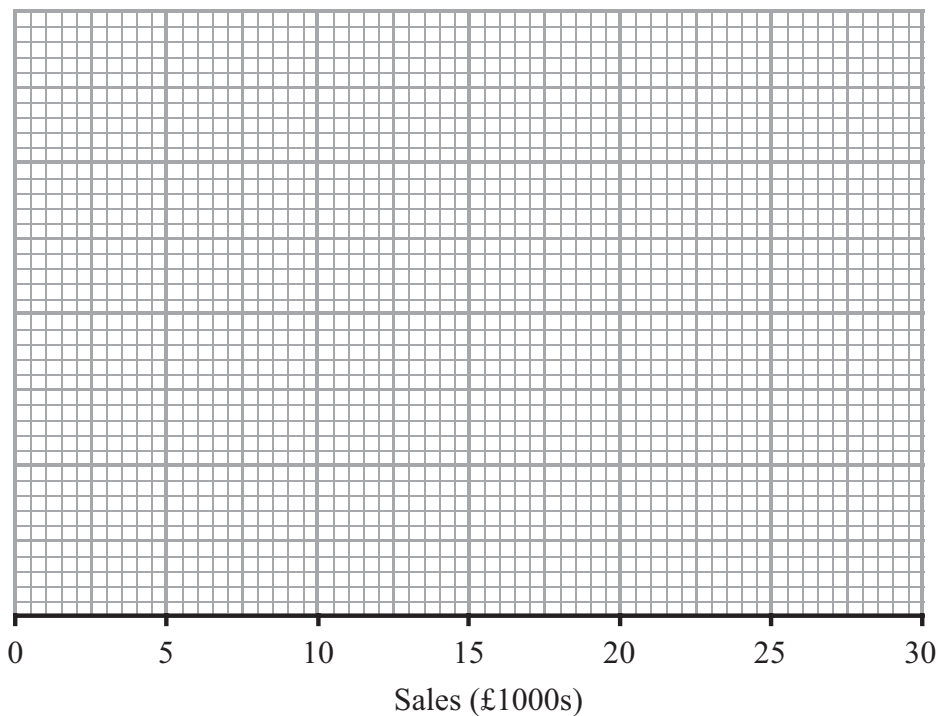
3. Over a long period of time a small company recorded the amount it received in sales per month. The results are summarised below.

| | Amount received in sales (£1000s) |
|--------------------|-----------------------------------|
| Two lowest values | 3, 4 |
| Lower quartile | 7 |
| Median | 12 |
| Upper quartile | 14 |
| Two highest values | 20, 25 |

An outlier is an observation that falls either $1.5 \times$ interquartile range above the upper quartile or $1.5 \times$ interquartile range below the lower quartile.

- (a) On the graph paper below, draw a box plot to represent these data, indicating clearly any outliers.

(5)



- (b) State the skewness of the distribution of the amount of sales received. Justify your answer.

(2)

- (c) The company claims that for 75% of the months, the amount received per month is greater than £10 000. Comment on this claim, giving a reason for your answer.

(2)



5. On a randomly chosen day, each of the 32 students in a class recorded the time, t minutes to the nearest minute, they spent on their homework. The data for the class is summarised in the following table.

| Time, t | Number of students |
|-----------|--------------------|
| 10 – 19 | 2 |
| 20 – 29 | 4 |
| 30 – 39 | 8 |
| 40 – 49 | 11 |
| 50 – 69 | 5 |
| 70 – 79 | 2 |

- (a) Use interpolation to estimate the value of the median. (2)

Given that

$$\sum t = 1414 \quad \text{and} \quad \sum t^2 = 69378$$

- (b) find the mean and the standard deviation of the times spent by the students on their homework. (3)
- (c) Comment on the skewness of the distribution of the times spent by the students on their homework. Give a reason for your answer. (2)



6. The discrete random variable X has the probability distribution

| | | | | |
|------------|-----|------|------|------|
| x | 1 | 2 | 3 | 4 |
| $P(X = x)$ | k | $2k$ | $3k$ | $4k$ |

(a) Show that $k = 0.1$ (1)

Find

(b) $E(X)$ (2)

(c) $E(X^2)$ (2)

(d) $\text{Var}(2 - 5X)$ (3)

Two independent observations X_1 and X_2 are made of X .

(e) Show that $P(X_1 + X_2 = 4) = 0.1$ (2)

(f) Complete the probability distribution table for $X_1 + X_2$ (2)

| | | | | | | | |
|--------------------|------|------|------|---|------|------|---|
| y | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| $P(X_1 + X_2 = y)$ | 0.01 | 0.04 | 0.10 | | 0.25 | 0.24 | |

(g) Find $P(1.5 < X_1 + X_2 \leq 3.5)$ (2)

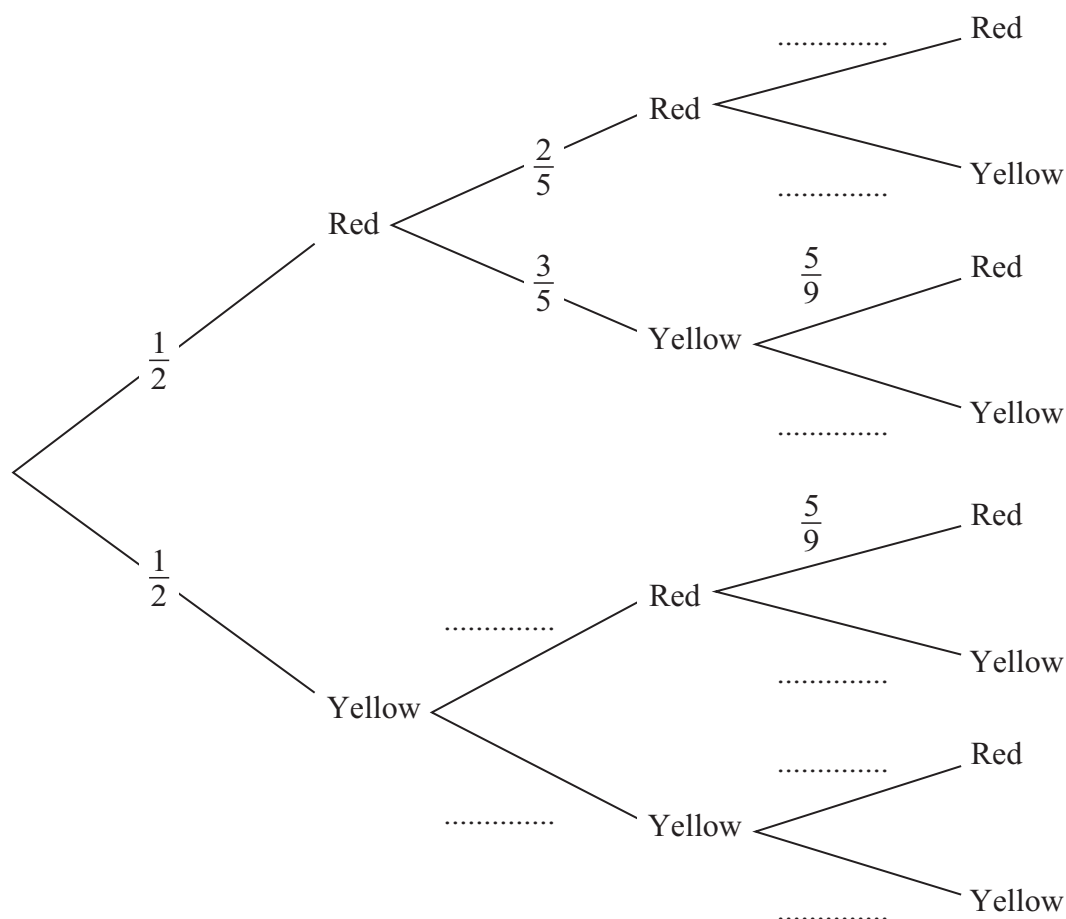


7. The bag P contains 6 balls of which 3 are red and 3 are yellow.
 The bag Q contains 7 balls of which 4 are red and 3 are yellow.
 A ball is drawn at random from bag P and placed in bag Q . A second ball is drawn at random from bag P and placed in bag Q .
 A third ball is then drawn at random from the 9 balls in bag Q .

The event A occurs when the 2 balls drawn from bag P are of the same colour.
 The event B occurs when the ball drawn from bag Q is red.

- (a) Complete the tree diagram shown below.

(4)



- (b) Find $P(A)$ (3)
- (c) Show that $P(B) = \frac{5}{9}$ (3)
- (d) Show that $P(A \cap B) = \frac{2}{9}$ (2)
- (e) Hence find $P(A \cup B)$ (2)
- (f) Given that all three balls drawn are the same colour, find the probability that they are all red. (3)



Question 7 continued

A large rectangular area filled with horizontal lines, intended for writing the answer to Question 7.

Q7

| | |
|--|--|
| | |
|--|--|

(Total 17 marks)



8. The weight, X grams, of soup put in a tin by machine A is normally distributed with a mean of 160 g and a standard deviation of 5 g.
A tin is selected at random.

(a) Find the probability that this tin contains more than 168 g. **(3)**

The weight stated on the tin is w grams.

(b) Find w such that $P(X < w) = 0.01$ **(3)**

The weight, Y grams, of soup put into a carton by machine B is normally distributed with mean μ grams and standard deviation σ grams.

(c) Given that $P(Y < 160) = 0.99$ and $P(Y > 152) = 0.90$ find the value of μ and the value of σ . **(6)**



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