

Centre No.						Paper Reference					Surname	Initial(s)
Candidate No.						<b>6</b>	<b>6</b>	<b>7</b>	<b>9</b>	/	<b>0</b>	<b>1</b>

### Paper Reference(s)

6679/01

# **Edexcel GCE**

# Mechanics M3

## **Advanced/Advanced Subsidiary**

## Friday 6 June 2008 – Afternoon

Time: 1 hour 30 minutes

## Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature.  
Check that you have the correct question paper.

Check that you have the correct question paper.  
Answer ALL the questions. Write your answers in the spaces provided in this question paper.

**Answer ALL the questions. Write your answers in the spaces provided in this question paper. If you need more space to complete your answer to any question, use additional answer sheets.**

If you need more space to complete your answer to any question  
Whenever a numerical value of  $g$  is required, take  $g = 9.8 \text{ m s}^{-2}$

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information for Candidates

A booklet ‘Mathematical Formulae and Statistical Tables’ is provided.

A booklet Mathematical Formulae and Statistical Tables is provided. Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets; e.g. (2).

The marks for individual questions and the parts of questions are shown in round brackets. There are 6 questions in this question paper. The total mark for this question paper is 75.

### Advice to Candidates

**Advice to Candidates**  
You must ensure that your answers to parts of questions are clearly labelled.

You must ensure that your answers to parts of questions are clearly labelled.  
You should show sufficient working to make your methods clear to the Examiner.

You should show sufficient working to make your answers gain full credit.

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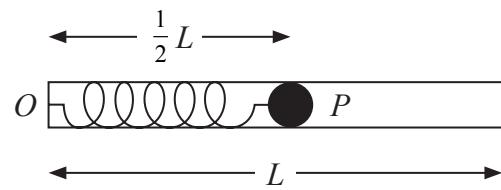
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*Turn over*

1.



**Figure 1**

A light elastic spring, of natural length  $L$  and modulus of elasticity  $\lambda$ , has a particle  $P$  of mass  $m$  attached to one end. The other end of the spring is fixed to a point  $O$  on the closed end of a fixed smooth hollow tube of length  $L$ .

The tube is placed horizontally and  $P$  is held inside the tube with  $OP = \frac{1}{2}L$ , as shown

in Figure 1. The particle  $P$  is released and passes through the open end of the tube with speed  $\sqrt{2gL}$ .

(a) Show that  $\lambda = 8mg$ .

(4)

The tube is now fixed vertically and  $P$  is held inside the tube with  $OP = \frac{1}{2}L$  and  $P$

above  $O$ . The particle  $P$  is released and passes through the open top of the tube with speed  $u$ .

(b) Find  $u$ .

(5)

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**Question 1 continued**

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**Q1**

**(Total 9 marks)**



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2. A particle  $P$  moves with simple harmonic motion and comes to rest at two points  $A$  and  $B$  which are 0.24 m apart on a horizontal line. The time for  $P$  to travel from  $A$  to  $B$  is 1.5 s. The midpoint of  $AB$  is  $O$ . At time  $t = 0$ ,  $P$  is moving through  $O$ , towards  $A$ , with speed  $u \text{ m s}^{-1}$ .

(a) Find the value of  $u$ .

(4)

(b) Find the distance of  $P$  from  $B$  when  $t = 2$  s.

(5)

(c) Find the speed of  $P$  when  $t = 2$  s.

(2)

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**Question 2 continued**

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**Q2**

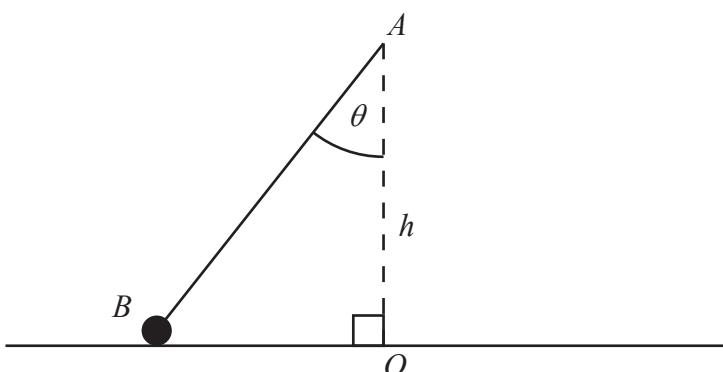
**(Total 11 marks)**



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3.



**Figure 2**

Figure 2 shows a particle  $B$ , of mass  $m$ , attached to one end of a light elastic string. The other end of the string is attached to a fixed point  $A$ , at a distance  $h$  vertically above a smooth horizontal table. The particle moves on the table in a horizontal circle with centre  $O$ , where  $O$  is vertically below  $A$ . The string makes a constant angle  $\theta$  with the downward vertical and  $B$  moves with constant angular speed  $\omega$  about  $OA$ .

- (a) Show that  $\omega^2 \leq \frac{g}{h}$ .

(8)

The elastic string has natural length  $h$  and modulus of elasticity  $2mg$ .

Given that  $\tan \theta = \frac{3}{4}$ ,

- (b) find  $\varphi$  in terms of  $g$  and  $h$ .

(5)

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### **Question 3 continued**

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**Q3**

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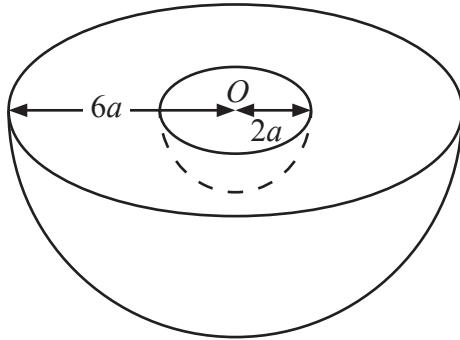


Figure 3

A uniform solid hemisphere, of radius  $6a$  and centre  $O$ , has a solid hemisphere of radius  $2a$ , and centre  $O$ , removed to form a bowl  $B$  as shown in Figure 3.

- (a) Show that the centre of mass of  $B$  is  $\frac{30}{13}a$  from  $O$ .

(5)

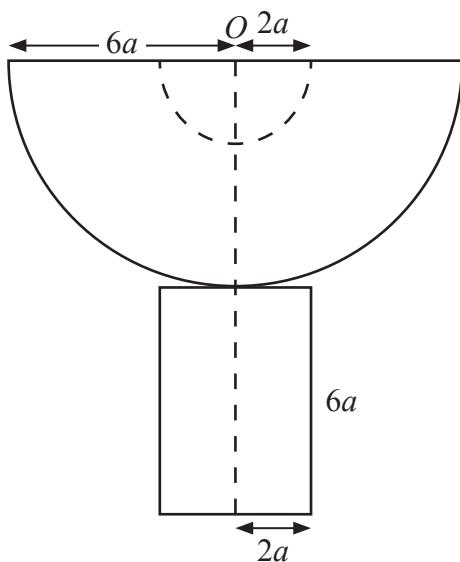


Figure 4

The bowl  $B$  is fixed to a plane face of a uniform solid cylinder made from the same material as  $B$ . The cylinder has radius  $2a$  and height  $6a$  and the combined solid  $S$  has an axis of symmetry which passes through  $O$ , as shown in Figure 4.

- (b) Show that the centre of mass of  $S$  is  $\frac{201}{61}a$  from  $O$ .

(4)

The plane surface of the cylindrical base of  $S$  is placed on a rough plane inclined at  $12^\circ$  to the horizontal. The plane is sufficiently rough to prevent slipping.

- (c) Determine whether or not  $S$  will topple.

(4)



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### **Question 4 continued**

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**Question 4 continued**

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**Q4**

**(Total 13 marks)**



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5. A particle  $P$  of mass  $m$  is attached to one end of a light inextensible string of length  $a$ . The other end of the string is attached to a fixed point  $O$ . The particle is released from rest with the string taut and  $OP$  horizontal.

(a) Find the tension in the string when  $OP$  makes an angle of  $60^\circ$  with the downward vertical.

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A particle  $Q$  of mass  $3m$  is at rest at a distance  $a$  vertically below  $O$ . When  $P$  strikes  $Q$  the particles join together and the combined particle of mass  $4m$  starts to move in a vertical circle with initial speed  $u$ .

(b) Show that  $u = \sqrt{\left(\frac{ga}{8}\right)}$ . (3)

The combined particle comes to instantaneous rest at  $A$ .

(c) Find

- (i) the angle that the string makes with the downward vertical when the combined particle is at  $A$ ,
  - (ii) the tension in the string when the combined particle is at  $A$ .

(6)



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## **Question 5 continued**

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**Question 5 continued**

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**Q5**

**(Total 15 marks)**



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6. A particle  $P$  of mass 0.5 kg moves along the positive  $x$ -axis. It moves away from the origin  $O$  under the action of a single force directed away from  $O$ . When  $OP = x$  metres, the magnitude of the force is  $\frac{3}{(x+1)^3}$  N and the speed of  $P$  is  $v$  m s $^{-1}$ .

Initially  $P$  is at rest at  $O$ .

(a) Show that  $v^2 = 6 \left( 1 - \frac{1}{(x+1)^2} \right)$ . (6)

(b) Show that the speed of  $P$  never reaches  $\sqrt{6} \text{ m s}^{-1}$ . (1)

(c) Find  $x$  when  $P$  has been moving for 2 seconds. (7)



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**Q6**

**(Total 14 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**

