

5. Sketch the graph of $y = \ln|x|$, stating the coordinates of any points of intersection with the axes.

(3)

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Question 5 continued

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(Total 3 marks)

Q5

13

Turn over



6.

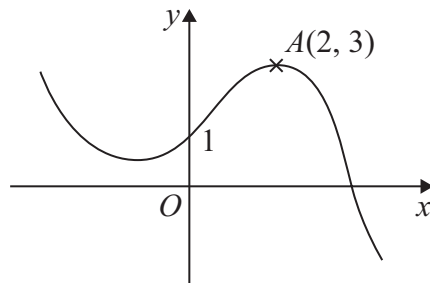


Figure 1

Figure 1 shows a sketch of the graph of $y = f(x)$.

The graph intersects the y -axis at the point $(0, 1)$ and the point $A(2, 3)$ is the maximum turning point.

Sketch, on separate axes, the graphs of

- (i) $y = f(-x) + 1$,
- (ii) $y = f(x + 2) + 3$,
- (iii) $y = 2f(2x)$.

On each sketch, show the coordinates of the point at which your graph intersects the y -axis and the coordinates of the point to which A is transformed.

(9)



Question 6 continued

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Question 6 continued

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Question 6 continued

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(Total 9 marks)

Q6





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7. (a) By writing $\sec x$ as $\frac{1}{\cos x}$, show that $\frac{d(\sec x)}{dx} = \sec x \tan x$. (3)

Given that $y = e^{2x} \sec 3x$,

(b) find $\frac{dy}{dx}$. (4)

The curve with equation $y = e^{2x} \sec 3x$, $-\frac{\pi}{6} < x < \frac{\pi}{6}$, has a minimum turning point at (a, b) .

(c) Find the values of the constants a and b , giving your answers to 3 significant figures. (4)



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Question 7 continued

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8. Solve

$$\operatorname{cosec}^2 2x - \cot 2x = 1$$

for $0 \leq x \leq 180^\circ$.

(7)

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9. (i) Find the exact solutions to the equations

(a) $\ln(3x - 7) = 5$

(3)

(b) $3^x e^{7x+2} = 15$

(5)

(ii) The functions f and g are defined by

$f(x) = e^{2x} + 3, \quad x \in \mathbb{R}$

$g(x) = \ln(x - 1), \quad x \in \mathbb{R}, x > 1$

(a) Find f^{-1} and state its domain.

(4)

(b) Find fg and state its range.

(3)



