June 2006 6686 Statistics S4 Mark Scheme

Question Number	Scheme	Marks
1.	Ho: 11 = 1012 Hi: 11 + 1012 Goth	BI
	$\bar{z} = \frac{13700}{14} \left(= 978.57 \right)$	MI .
	$S_{x^{2}} = \frac{13 \ 448 \ 750 \ -145c^{2}}{13} = \frac{3255.49}{(S_{x} = 57.056)} S^{2}_{x}S$	
	$t_{13} = \frac{\bar{x} - \mu}{57.0} = \frac{978.6 - 1012}{57.0} = -2.19$ Awar - 2.19	··· \
	$t_{13}(5\%)$ 2 tail c.v. = -2-160	/ /
	Significant roult - there is evidence of a change in mean weight of squared (condone decrease) must mention weight	AIT (7)
2.	(a) $(\bar{z} = \frac{466}{4} = 116.5)$ $S_{2}^{2} = \frac{54386}{3} - 4\bar{z}^{2}$, $= \frac{32.3}{3} = \frac{97}{3}$	HI, AI
~.	$0.216 < \frac{3 \text{ Sx}^2}{55^2} < 9.248$	BI HI GI
	10.376 < 52 < 449.07 AWRT 10.4,1449	
in die er i er i er i er die de	(b) Ho: $6m^2 = 6s^2$ H ₁ : $6m^2 > 6s^2$ (one ok)	ßı
	$\frac{S_{N}^{2}}{S_{s}^{2}} = \frac{318.8}{31.3} = 9.851$ AWRT 9.86	MI AI
. 3	F _{6.3} (1% c.v.) = 27.91	G1
-4	9.85 < 2791, Insufficient evidence of an increase in variance to say on 270, 2 nok. Variance can be assumed to be the same 60K	AIJ (5)
(G)	NA 32.3 = 0.101 only gets MIAI if appropriate Fralse attempted]	

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Question Number	Scheme Mishiek is	
3.	(D = Without Solar heating - With Solar heating) [= 0 300	60
(a)		B1
	A: 6, -3, 7, -2, -8, 6, 9, 11, 9	MI
	$\vec{d} = 3$, $S\lambda = 6$ $\left(= \int \frac{369 - 9 \times 3^{\frac{1}{4}}}{9} \right) \left(\frac{2d}{9} \right)^{M_1}$	
	$t_8 = \frac{3-0}{4\pi} = 1.5$ (±)	MIAI cao
	to (5% Itail C.v.) = 1.860	ßı \
	Not significant - insufficient evidence (that solar heating has) decreased weekly fuel consumption.	ALT (8)
(4)	and the state of t	(1)
1, (2)	(Ho: 6A2 = 602 Hi: 6A2 + 6B2)	
4. (4)	$\frac{S_{A}^{2}}{S_{a}^{2}} = \frac{0.721^{2}}{0.572} = [.529$ Awar 1.59	MI AI
	Sg2 0.572 F8,9 (576) C.V. [= 1076 2 kmi] = 3.23	ונו
	Not significant, can assume variances are copsal. (accept of 2= 502)	B1 cac(4)
(6)	0-417	ні аі
	617 (2.5%) cv. = 2-110	31
		Mi
	95% CI = 26-274 ± 2-110 × SAX = + 10 = 0.02 ± 2-110 × \overline \square \frac{1}{4} + \frac{1}{10}	AL.
	= (-0.6066) AWRT (-0.607,064	A1, A1 (7)
(c)	+ 0.7 is outside internal	$a_i f$
	± 0.7 is outside internal . manager need not be concerned (dep) (allow J if 0.7 inside)	(2) (3)

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X,= no. of defects in 15 m . X, ~ Po (4.5)
                                                                          Useof Po(4.5)
5 (4)
           Size = P(X, >9) = 1-P(X 58) = 1-0.9597 = 0.0403 (AWRT) A1
                                                                                                     (2)
     (4) | r = P(X2>9 | X2P.(9),= 1-P(X258)=1-0.4557 = 0.54 (43) (43) MI, AI
                                                                                                     (2)
                                                           West Po (3) to find P(Y2) MI
     (c) Y, = no. of defect, in 10m Y, ~ Po (3)
          Require smallest c so that P(Y, >c) <0.10. Tables
                                                                                             A١
                                                                                                     (2)
     (d) Size = P(Y, >6) = 1-P(Y, 55) = 1-0.9161 = 0.0839
                                                                                                     (ı)
                                                                                             ß١
      (e) S = 1 - P(Y2 55 | Y2~P0(8)), = 1-0-1912 = 0.8088 (ALLETO-81) HI, AI
                                                                                                      (2)
                                                                                            (4)<sub>2</sub>
                                                                                                      (4)
            See graph
      (<del>f</del>)
                                                                                            B1 B1
                                                                                                      (2)
                                               (ii) Test I is more powerful
             (i) 0.62 ~ 0.67
      (9)
      (h) Test 2 has higher P(Type I error) but cont of this is low
                                                                                            BI Tota
            Test 2 is More powerful for 2 <0.7 and 2 >0.7 is rare
                                                                                            BI Resson (2)
                                                                                                  (17)
 6. (a) E(x^n) = \int_0^t x^n \frac{1}{t} dx = \left[\frac{x^{n+1}}{t^{(n+1)}}\right]_0^t = \left(\frac{t^{n+1}}{t^{(n+1)}} - 0\right) = \frac{t^n}{n+1} \int_0^t dx
                                                                                                  Al čio
                                                                                                      (3)
      (b) (E(x) = \frac{1}{2}) E(s) = kE(x)E(x) , = k. \frac{1}{4}
                                                                                             MI, AI
                                                                                            A I
                                                                                                      (3)
      (c) Var (xY) = E(x2) E(Y2) - [E(xY)]2
                                                                                            нı
             = \frac{\xi^{2}}{3} \times \frac{\xi^{2}}{3} - \left(\frac{\xi^{2}}{4}\right)^{2} = \left\{\frac{7\xi^{4}}{144}\right\}
Var(s) = k^{2} Var(xy) = \frac{16 \times 7\xi^{4}}{144} = \frac{7\xi^{6}}{7}
                                                                                             MI
                                                                                            Al cro (3)
       (d) E(u) = t^1 \Rightarrow \lambda E(x^1)q = t^2, \Rightarrow \lambda \frac{t^1}{3}q = t^2, \Rightarrow q = \frac{3}{2}
                                                                                             MI, MI, Alcio
       (e) Var(u) = q2 [Var(x2) + Var(Y2)] = 2q2 Var(x2)
                                                                                            HI
            Var(x2) = E(x4) - [E(x2)]2 = = = = (4 t4)
                                                                                            MI
                                                                                             Αl
                                                                                                      (3)
           Var(u) = 2×9×45 +4 = 3+4
                                                                                             BIN
                                                                                                      (1)
       (f) 2 < 7 : un better : smaller variance
       (g) Using u estimate is: \(\frac{2}{3}\)(22+32) = \(\frac{2}{2}\)x13 = \(\frac{2}{3}\) or 19.5
                                                                                             BIJ
                                                                                                      (0)
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