

1. A particle A has constant velocity $(3\mathbf{i} + \mathbf{j}) \text{ m s}^{-1}$ and a particle B has constant velocity $(\mathbf{i} - \mathbf{k}) \text{ m s}^{-1}$. At time $t = 0$ seconds, the position vectors of the particles A and B with respect to a fixed origin O are $(-6\mathbf{i} + 4\mathbf{j} - 3\mathbf{k}) \text{ m}$ and $(-2\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}) \text{ m}$ respectively.

(a) Show that, in the subsequent motion, the minimum distance between A and B is $4\sqrt{2} \text{ m}$.

(6)

(b) Find the position vector of A at the instant when the distance between A and B is a minimum.

(2)



Question 1 continued

Lined area for writing the answer to Question 1.

Q1

(Total 8 marks)



2. A car of mass 1000 kg is moving along a straight horizontal road. The engine of the car is working at a constant rate of 25 kW . When the speed of the car is $v\text{ m s}^{-1}$, the resistance to motion has magnitude $10v\text{ newtons}$.

(a) Show that, at the instant when $v = 20$, the acceleration of the car is 1.05 m s^{-2} . (3)

(b) Find the distance travelled by the car as it accelerates from a speed of 10 m s^{-1} to a speed of 20 m s^{-1} . (8)



Question 2 continued

Lined area for writing the answer to Question 2.

Q2

(Total 11 marks)

--	--



Question 4 continued

This section contains 33 horizontal lines for writing your answer to Question 4.



Question 4 continued

Lined writing area for the answer to Question 4.

(Total 8 marks)

Q4



P 4 3 1 5 9 A 0 1 1 2 4

5.

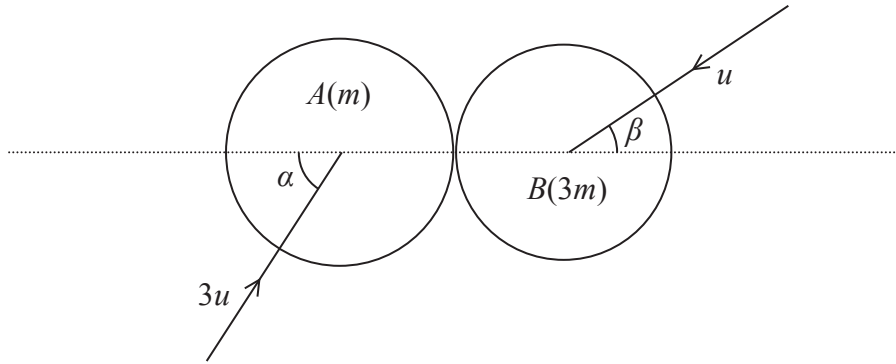


Figure 1

Two smooth uniform spheres A and B have equal radii. The mass of A is m and the mass of B is $3m$. The spheres are moving on a smooth horizontal plane when they collide obliquely. Immediately before the collision, A is moving with speed $3u$ at angle α to the line of centres and B is moving with speed u at angle β to the line of centres, as shown in Figure 1. The coefficient of restitution between the two spheres is $\frac{1}{5}$. It is given that $\cos\alpha = \frac{1}{3}$ and $\cos\beta = \frac{2}{3}$ and that α and β are both acute angles.

- (a) Find the magnitude of the impulse on A due to the collision in terms of m and u . (8)

- (b) Express the kinetic energy lost by A in the collision as a fraction of its initial kinetic energy. (4)

6. A particle of mass m kg is attached to one end of a light elastic string of natural length a metres and modulus of elasticity $5ma$ newtons. The other end of the string is attached to a fixed point O on a smooth horizontal plane. The particle is held at rest on the plane with the string stretched to a length $2a$ metres and then released at time $t=0$. During the subsequent motion, when the particle is moving with speed v m s⁻¹, the particle experiences a resistance of magnitude $4mv$ newtons. At time t seconds after the particle is released, the length of the string is $(a+x)$ metres, where $0 \leq x \leq a$.

(a) Show that, from $t = 0$ until the string becomes slack,

$$\frac{d^2x}{dt^2} + 4 \frac{dx}{dt} + 5x = 0 \quad (3)$$

(b) Hence express x in terms of a and t .

(6)

(c) Find the speed of the particle at the instant when the string first becomes slack, giving your answer in the form ka , where k is a constant to be found correct to 2 significant figures.

(4)



7.

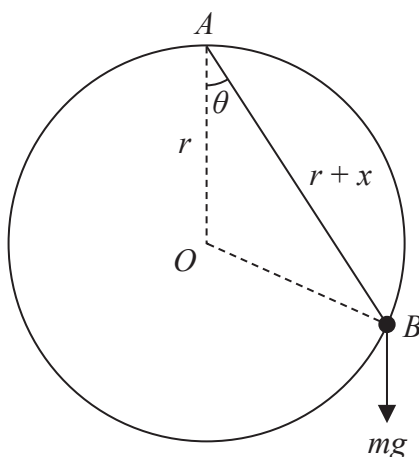


Figure 2

A bead B of mass m is threaded on a smooth circular wire of radius r , which is fixed in a vertical plane. The centre of the circle is O , and the highest point of the circle is A . A light elastic string of natural length r and modulus of elasticity kmg has one end attached to the bead and the other end attached to A . The angle between the string and the downward vertical is θ , and the extension in the string is x , as shown in Figure 2.

Given that the string is taut,

(a) show that the potential energy of the system is

$$2mgr\{(k-1)\cos^2\theta - k\cos\theta\} + \text{constant} \tag{6}$$

Given also that $k=3$,

(b) find the positions of equilibrium and determine their stability. (9)



