



Question 1 continued

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Lined area for writing the answer to Question 1.

(Total 6 marks)

Q1



2.

$$\mathbf{M} = \begin{pmatrix} 1 & p & 2 \\ 0 & 3 & q \\ 2 & p & 1 \end{pmatrix},$$

where p and q are constants.

Given that $\begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}$ is an eigenvector of \mathbf{M} ,

(a) show that $q = 4p$. **(3)**

Given also that $\lambda = 5$ is an eigenvalue of \mathbf{M} , and $p < 0$ and $q < 0$, find

(b) the values of p and q , **(4)**

(c) an eigenvector corresponding to the eigenvalue $\lambda = 5$. **(3)**





Question 2 continued

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Question 4 continued

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N 3 0 0 2 5 A 0 1 3 2 8





Question 4 continued

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Question 4 continued

Lined writing area for the answer to Question 4.

(Total 12 marks)

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Q4

15

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5.
$$\mathbf{A} = \begin{pmatrix} k & -2 \\ 1-k & k \end{pmatrix},$$
 where k is constant.

A transformation $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$ is represented by the matrix \mathbf{A} .

- (a) Find the value of k for which the line $y = 2x$ is mapped onto itself under T . (3)
- (b) Show that \mathbf{A} is non-singular for all values of k . (3)
- (c) Find \mathbf{A}^{-1} in terms of k . (2)

A point P is mapped onto a point Q under T .

The point Q has position vector $\begin{pmatrix} 4 \\ -3 \end{pmatrix}$ relative to an origin O .

Given that $k = 3$,

- (d) find the position vector of P . (3)



7.

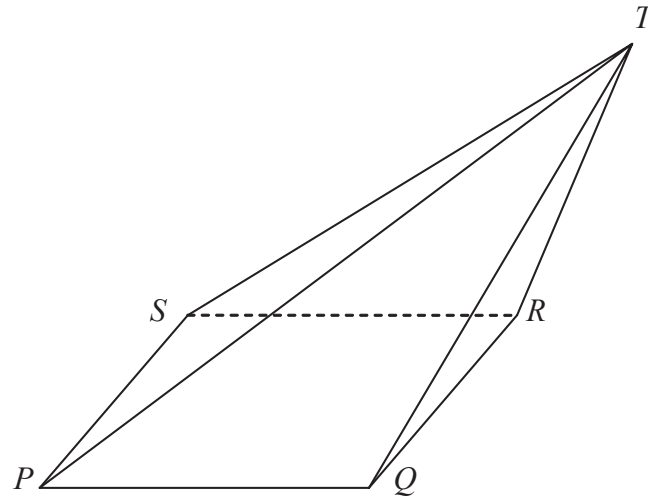


Figure 1

Figure 1 shows a pyramid $PQRST$ with base $PQRS$.

The coordinates of P , Q and R are $P(1, 0, -1)$, $Q(2, -1, 1)$ and $R(3, -3, 2)$.

Find

(a) $\overrightarrow{PQ} \times \overrightarrow{PR}$, (3)

(b) a vector equation for the plane containing the face $PQRS$, giving your answer in the form $\mathbf{r} \cdot \mathbf{n} = d$. (2)

The plane Π contains the face PST . The vector equation of Π is $\mathbf{r} \cdot (\mathbf{i} - 2\mathbf{j} - 5\mathbf{k}) = 6$.

(c) Find cartesian equations of the line through P and S . (5)

(d) Hence show that PS is parallel to QR . (2)

Given that $PQRS$ is a parallelogram and that T has coordinates $(5, 2, -1)$,

(e) find the volume of the pyramid $PQRST$. (3)



Question 7 continued

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